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Brown's speculation about spaces of R-places of function fields over non-archimedean real closed fields

It is well known that the space of all $\mathbb{R}$-places of a rational function field $R(X)$ over an archimedean real closed field R is homeomorphic to the circle. Manfred Knebusch proved in 1976 that the space of $\mathbb{R}$-places of a finite extension of $R(X)$ is homeomorphic to a finite disjoint union of circles, and Ron Brown generalized this in 1980 to the case of any archimedean ordered field R. In the same paper he suggested that an analogue holds in the non-archimedean case, namely, that the space of $\mathbb{R}$-places of a finite extension is a finite disjoint union of copies of the space of $\mathbb{R}$-places of the rational function field. We have recently determined the structure of the latter. But an example that we will discuss appears to show that Brown's suggestion fails; details have yet to be worked out.